



STATISTICS: A FOUNDATION FOR INNOVATION

Maximin Optimal Cluster Randomized Designs Accounting for Treatment Effect Heterogeneity

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Introduction

- Cluster randomized trials (CRT): treatment randomized at cluster level; outcomes (typically) collected at individual level
- Heterogeneous treatment effects (HTE): effect modifiers driving variations in a patient's response to interventions

Cluster treatment indicator

(1)

$$Y_{ij} = \beta_1 + \beta_2 W_i + \beta_3 X_{ij} + \beta_4 X_{ij} W_i + \gamma_i + \epsilon_{ij}$$

Individual covariate
HTE

- **Confirmatory** HTE analyses must be pre-specified
 - Little guidance on **how to power** these analyses when we are uncertain about the outcome ICC, $\rho_{y|x}$, and covariate ICC, ρ_x

(2)

$$\text{var}(\widehat{\beta}_4) = \sigma_{HTE}^2 = \frac{\sigma_{y|x}^2 (1 - \rho_{y|x}) \{1 + (m + 1) \rho_{y|x}\}}{\# \text{ clusters } n m \sigma_w^2 \sigma_x^2 \{1 + (m - 2) \rho_{y|x} - (m - 1) \rho_x \rho_{y|x}\}}$$

Outcome ICC
Covariate ICC

[Yang et al.,(2020)]

Knowledge Gaps

1. What formulations of cluster size m and number of clusters n will **minimize** σ_{HTE}^2 , with respect to a budget constraint, when ICCs are known?
2. When **ICCs are not known**, can we find a (m, n) design that will be most efficient among scenarios of inefficient ICC combinations?
3. Is there a way to adequately power a CRT for **both** HTE and average treatment effect (ATE) analyses?

Application to the K-DPP Study

Kerala Diabetes Prevention Program

[Thankappan et al., 2018]

- CRT of peer-support lifestyle diabetes intervention
- Secondary outcome: change in Indian Diabetes Risk Score
 - Post-hoc HTE: IDRS interaction with BMI
- 60 clusters with 10-23 participants each

RESEARCH ARTICLE

A peer-support lifestyle intervention for preventing type 2 diabetes in India: A cluster-randomized controlled trial of the Kerala Diabetes Prevention Program

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Abstract

Background

The major efficacy trials on diabetes prevention have used resource-intensive approaches to identify high-risk individuals and deliver lifestyle interventions. Such strategies are not feasible for wider implementation in low- and middle-income countries (LMICs). We aimed to evaluate the effectiveness of a peer-support lifestyle intervention in preventing type 2 diabetes among high-risk individuals identified on the basis of a simple diabetes risk score.

Methods and findings

The Kerala Diabetes Prevention Program was a cluster-randomized controlled trial conducted in 60 polling areas (clusters) of Neyyattinkara taluk (sub-district) in Trivandrum district, Kerala state, India. Participants (age 30–60 years) were those with an Indian Diabetes Risk Score (IDRS) ≥ 60 and were free of diabetes on an oral glucose tolerance test (OGTT). A total of 1,007 participants (47.2% female) were enrolled (507 in the control group and 500 in the intervention group). Participants from intervention clusters participated in a 12-month



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KG1: HTE Locally Optimal Design

KG1: What formulations of cluster size m and number of clusters n will minimize σ_{HTE}^2 , with respect to a budget constraint, when ICCs are known?

- Locally optimal design (LOD): design that maximizes power/minimizes variance **under budget constraints** for fixed values of design parameters
- Budget constraint:

$$\begin{aligned}
 (3) \quad & \begin{array}{l} \text{per-cluster} \quad \text{per-subject} \\ \text{cost} \quad \quad \quad \text{cost} \\ B = \boxed{cn} + \boxed{smn} \\ \quad \quad \quad = n(c + sm) \end{array} \Rightarrow \boxed{n = \frac{B}{c + sm}} \quad \begin{array}{l} \text{Replace } n \text{ in} \\ \sigma_{\text{HTE}}^2 \text{ and} \\ \text{minimize for } m \end{array}
 \end{aligned}$$

KG1: HTE Locally Optimal Design

Proposition 1 - Minimizing σ_{HTE}^2 with respect to m , the HTE LOD for a given minimum number of clusters, \underline{n} , is:

i. If $\frac{\rho_{y|x}(k+1)}{\rho_{y|x}^{k+1}} < \rho_x \leq 1$ and $m_{\text{opt}} \leq \frac{B/\underline{n}-c}{s}$

(4)
$$m_{\text{opt}} = \frac{(1 - \rho_{y|x})(1 - \rho_x) + \sqrt{\rho_{y|x}^{-1} k^{-1} (1 - \rho_{y|x})(\rho_x - \rho_{y|x}) \{1 - (k + 2)\rho_{y|x} + k + 1\} \rho_x \rho_{y|x}}}{k^{-1}(\rho_x - \rho_{y|x}) - \rho_{y|x}(1 - \rho_x)}$$

Only depends on cost ratio (c/s)

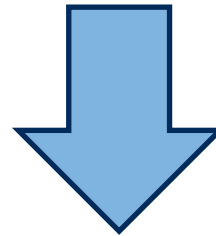
ii. Otherwise

$$m_{\text{opt}} = \frac{B/\underline{n} - c}{s}$$

$$n_{\text{opt}} = \frac{B}{c + sm_{\text{opt}}}$$

KG1: Application to K-DPP

- Intervention cluster- to -individual cost ratio $k \approx 30$
 - Accounting for cheaper control arm, assume $k = 20$ and $B = \$20,000$
- $\Delta_{IDRS} = -1.5; \Delta_{HTE} = 0.25 \times \Delta_{IDRS} = -0.375$
- $\rho_{y|x} = 0.028, \rho_x = 0.055$



- If minimum of 66 clusters (maximum m of 40):

$$\text{LOD: } m_{opt} = 40, n_{opt} = 66$$

KG2: HTE Maximin Design

- LOD requires **fixed/known ICCs** – unrealistic expectation

KG2: When ICCs are not known, can we find a (m, n) design that will be most efficient among scenarios of inefficient ICC combinations?

- Maximin designs (MMD): design that is highly efficient in worst case parameter scenarios [van Breukelen and Candel, 2015]
- Comparing designs (m, n) based on **relative efficiency** compared to LOD at a specific $(\rho_{y|x}, \rho_x)$ combination:

$$RE_{HTE} = \frac{\sigma_{HTE}^{2*}}{\sigma_{HTE}^2}$$

HTE variance under
LOD($\rho_{y|x}, \rho_x$)

HTE variance at (m, n)
and $(\rho_{y|x}, \rho_x)$

KG2: HTE Maximin Design

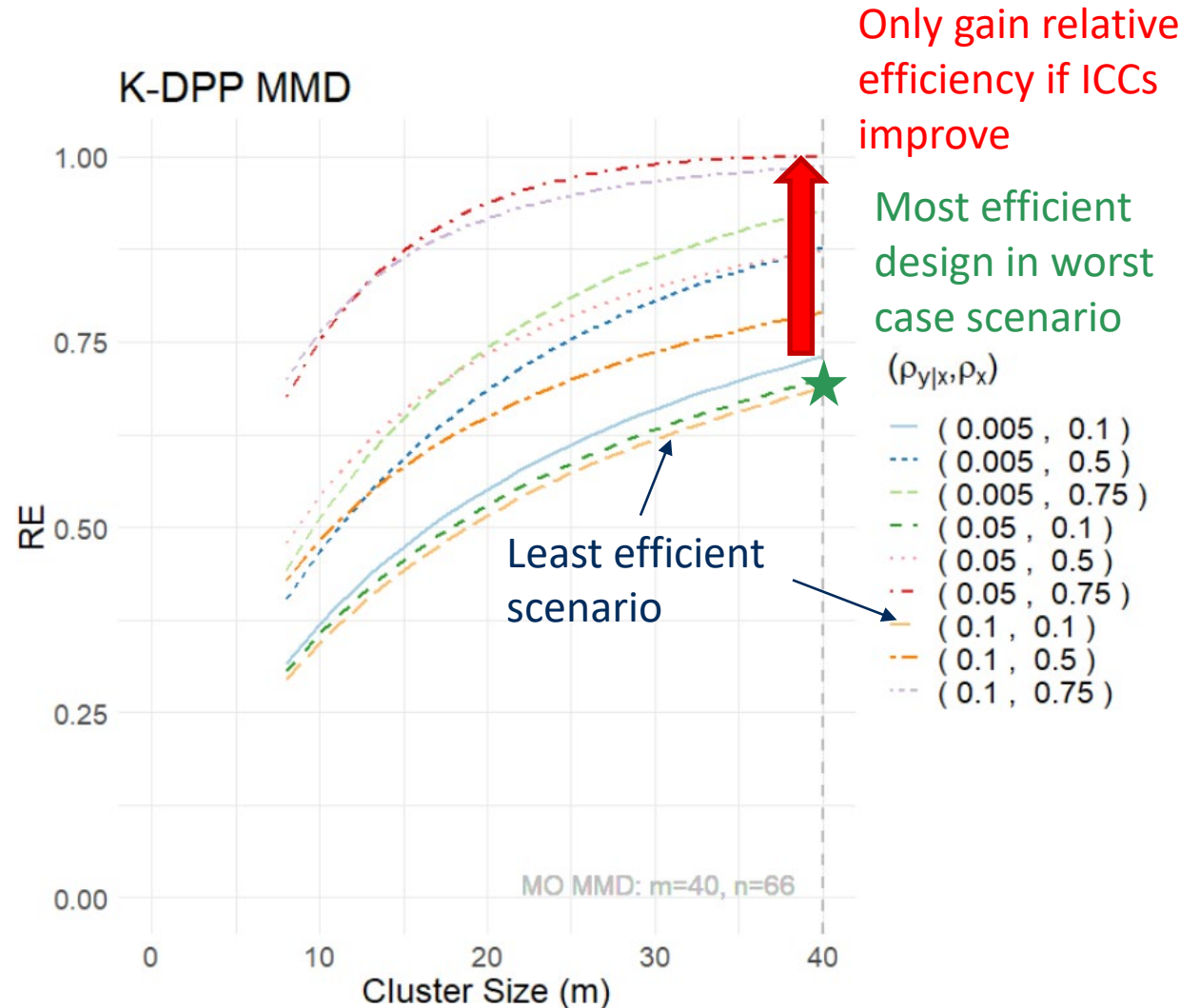
MMD for assessing HTE in CRTs

1. Define the parameter space $(\rho_{y|x}, \rho_x)$ and design space $(m, n(m))$
2. For each $(\rho_{y|x}, \rho_x)$, compute HTE LOD according to (5). Then compute RE for each $(m, n(m))$ compared with the LOD at the $(\rho_{y|x}, \rho_x)$
3. For each $(m, n(m))$, identify the $(\rho_{y|x}, \rho_x)$ with the **smallest RE**
4. Among the smallest REs, choose the $(m, n(m))$ with the **largest RE**

KG2: Application to K-DPP

- $m \in [8, 40]$
- $n \in [66, 143]$
- $\rho_{y|x} \in [0.005, 0.1]$
- $\rho_x \in [0.1, 0.75]$

MMD: $m_{opt} = 40, n_{opt} = 66$
 96.7% power to detect Δ_{HTE}
 under least efficient scenario
 96.5% power to detect Δ_{HTE}
 under actual ICCs (0.03, 0.06)



KG3: Compound Objective

KG3: Is there a way to adequately power a CRT for both HTE and average treatment effect (ATE) analyses?

- Optimal designs for assessing HTE (minimizing σ_{HTE}^2) may not be optimal for assessing ATE (minimizing σ_{ATE}^2)
- Need **compound criterion** to optimize over that takes both HTE and ATE objectives into account

Weighted combo of
single objective REs

$$(6) \quad \Theta(\zeta|\lambda) = \lambda \frac{\Theta_{\text{ATE}}(\zeta_{\text{ATE}}^*)}{\Theta_{\text{ATE}}(\zeta)} + (1 - \lambda) \frac{\Theta_{\text{HTE}}(\zeta_{\text{HTE}}^*)}{\Theta_{\text{HTE}}(\zeta)}$$

LOD under ATE
HTE variance under design ζ

Priority weight

KG3: Compound Maximin

- When there is uncertainty around ICC values:

Compound MMD for assessing HTE and ATE in CRTs

1. Choose priority weight λ
2. Define the parameter space $(\rho_{y|x}, \rho_x)$ and design space $(m, n(m))$
3. For each $(\rho_{y|x}, \rho_x)$, compute the LOD for each objective. Then compute $\Theta(\zeta|\lambda)$ for each $(m, n(m))$ compared with their LODs at the $(\rho_{y|x}, \rho_x)$
4. For each $(m, n(m))$, identify the $(\rho_{y|x}, \rho_x)$ with the **smallest criterion value**
5. Among the smallest criterion values, choose the $(m, n(m))$ with the **largest criterion value**

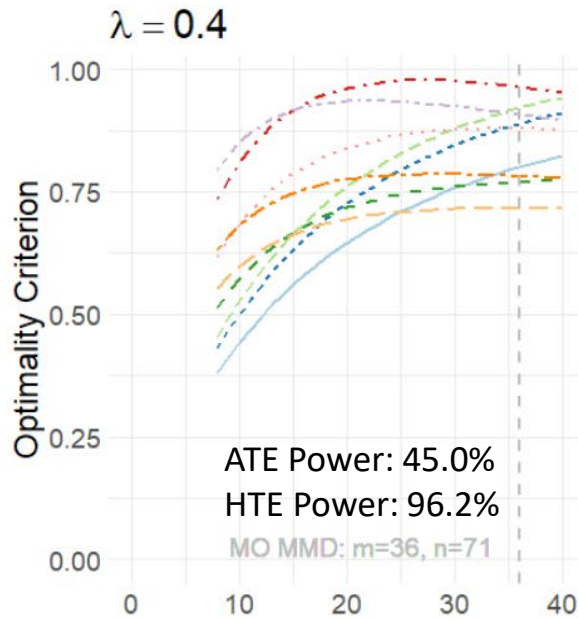
KG3: Application to K-DPP

- $m \in [8, 40]$
- $n \in [66, 143]$

- $\rho_{y|x} \in [0.005, 0.1]$
- $\rho_x \in [0.1, 0.75]$

Calculate power under the worse of the intersecting ICC scenarios

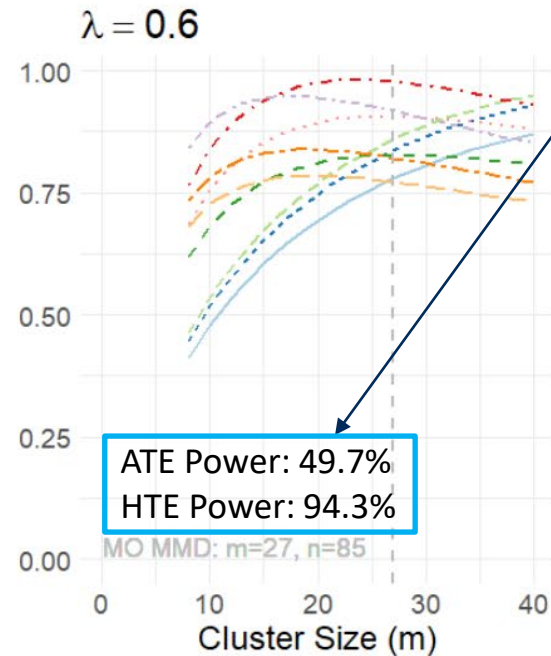
K-DPP MO MMD



Power under actual ICCs (0.03, 0.06)

ATE: 76.0%

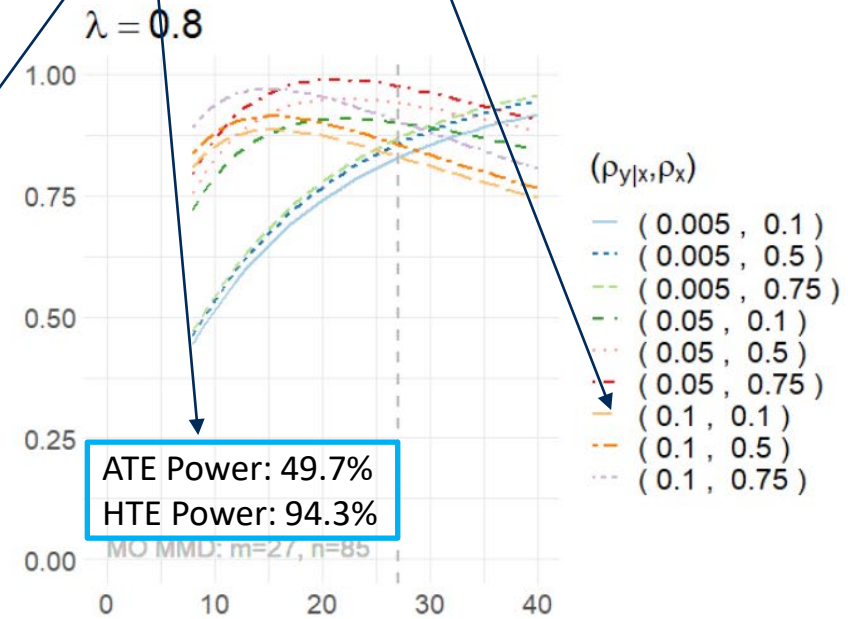
HTE: 96.0%



Power under actual ICCs (0.03, 0.06)

ATE: 77.2%

HTE: 94.1%



Power under actual ICCs (0.03, 0.06)

ATE: 77.2%

HTE: 94.1%

Online Application

Locally Optimal and Maximin Designs for Cluster Randomized Trials

Type of Objective:
 Single objective - HTE
 Single Objective - ATE
 Multiple Objective

LOD or MMD?
 LOD
 MMD

Total budget: 100000
Cost per cluster: 500
Cost per participant: 50

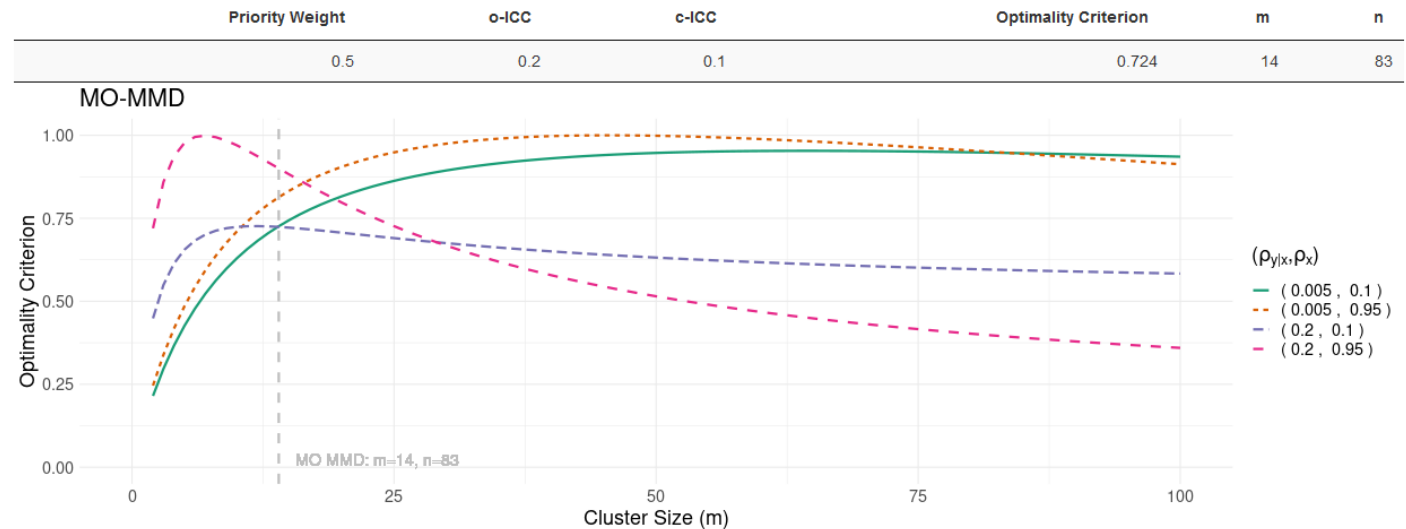
Min. o-ICC: 0.005
Max. o-ICC: 0.2

Min. c-ICC: 0.1
Max. c-ICC: 0.95

Min. Number of Clusters (n): 6
Max. Number of Clusters (n): 100

Min. Cluster Size (m): 2
Max. Cluster Size (m): 100

Priority weight: 0.5



Shiny App: <https://mary-ryan.shinyapps.io/HTE-MMD-app/>

Conclusions

- Understanding treatment effect heterogeneity **crucial for improving how and to whom** future interventions can be designed and delivered
- Optimal designs **free of effect size** within budget constraint
- Possible to find maximin designs **robust** to ICC value misspecification that jointly consider **both** HTE and ATE objectives

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Thank you!

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Shiny App: <https://mary-ryan.shinyapps.io/HTE-MMD-app/>

Questions?

KG3.1: Compound LOD

- When ICCs are known, find compound LOD by solving for m that **maximizes** $\Theta(\zeta|\lambda)$

$$\begin{aligned}
 \max_m \Theta(\zeta|\lambda) &= \lambda \frac{\Theta_{ATE}(\zeta_{ATE}^*)}{\Theta_{ATE}(\zeta)} + (1 - \lambda) \frac{\Theta_{HTE}(\zeta_{HTE}^*)}{\Theta_{HTE}(\zeta)} \\
 &= \frac{W_{ATE}}{\sigma_{ATE}^2} + \frac{W_{HTE}}{\sigma_{HTE}^2}
 \end{aligned}$$

Appendix: Compound LOD

Proposition 2 - Locally optimal compound design

i. If $w_{ATE} > w_{HTE} \{ (k + 1)\rho_{y|x} - \rho_x(k\rho_{y|x} + 1) \}$ and $m_{opt} \leq \frac{B/\underline{n} - c}{s}$

$$(A1) \quad m_{opt} = \frac{-w_{HTE}ka_2 - \sqrt{w_{HTE}^2k^2a_2^2 - 4\{w_{HTE}(ka_1 - b_1) - w_{ATE}\rho_{y|x}\}\{w_{ATE}k(1 - \rho_{y|x}) + w_{HTE}ka_3\}}}{2\{w_{HTE}(ka_1 - b_1) - w_{ATE}\rho_{y|x}\}}$$

Constants
involving
 ρ_x and $\rho_{y|x}$

$$n_{opt} = \frac{B}{c + sm_{opt}}$$

ii. Otherwise

$$m_{opt} = \frac{B/\underline{n} - c}{s}$$

$$n_{opt} = \frac{B}{c + sm_{opt}}$$

Appendix: Compound LOD

- Extraneous terms in (A1):

$$a_1 = \rho_{y|x}^2(1 - \rho_x)$$

$$a_2 = 2\rho_{y|x}(1 - \rho_{y|x})(1 - \rho_x)$$

$$a_3 = (1 - 2\rho_{y|x} + \rho_x\rho_{y|x})(1 - \rho_{y|x})$$

$$b_1 = \rho_{y|x}(\rho_x - \rho_{y|x})$$